

# How to Act as Team

## Multi-Robot Coordination

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Bernhard Rinner

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# Acknowledgements

- Pervasive Computing group  
<https://www.bernhardrinner.com>



- Dronehub Klagenfurt  
<https://uav.aau.at>



# Team Behavior of Multiple Robots

- Coordinate actions in space and time to achieve common goal
- Key coordination tasks include
  - Sharing of knowledge
  - Joint decision making
  - Resource allocation
- Complex problem with huge design space
  - Various constraints: energy, communication, deadlines, payloads etc.
  - Multiple objectives: mission, QoS, resource-efficiency
  - Different realizations: offline/online, centralized/distributed,
- Highly relevant for many MRS applications, eg.,
  - Entertainment, monitoring/inspection, search&rescue, transportation



# Two Examples of Team Behavior



## Multi-drone constellation change

- Collision-free trajectory planning with MPC path following
- Framed as optimization problem with various constraints
- Offline coordination

[Ladinig et al. Time and Energy Optimized Trajectory Generation for Multi-Agent Constellation Changes. In *Proc. ICRA*, 2021.]

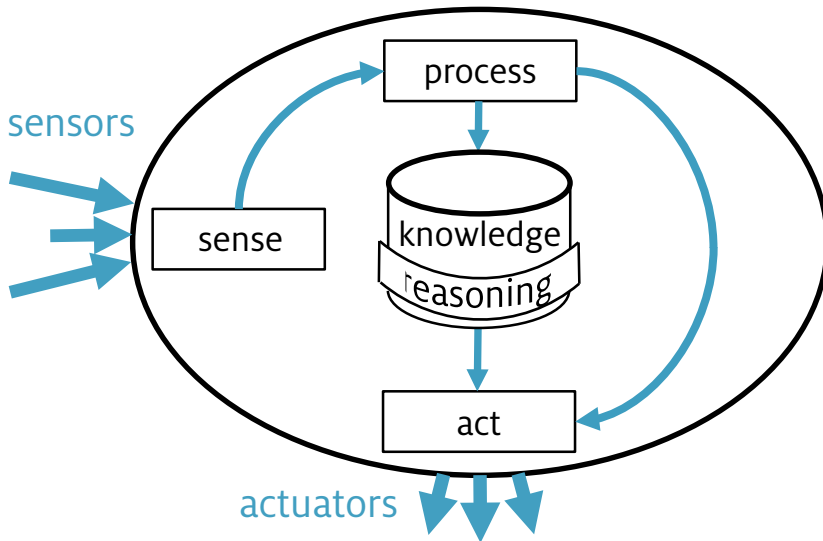


## Swarming and synchronization

- Collective behavior emerges from local processing and interaction
- Following self-organization principles („swarmalators“)
- Online coordination

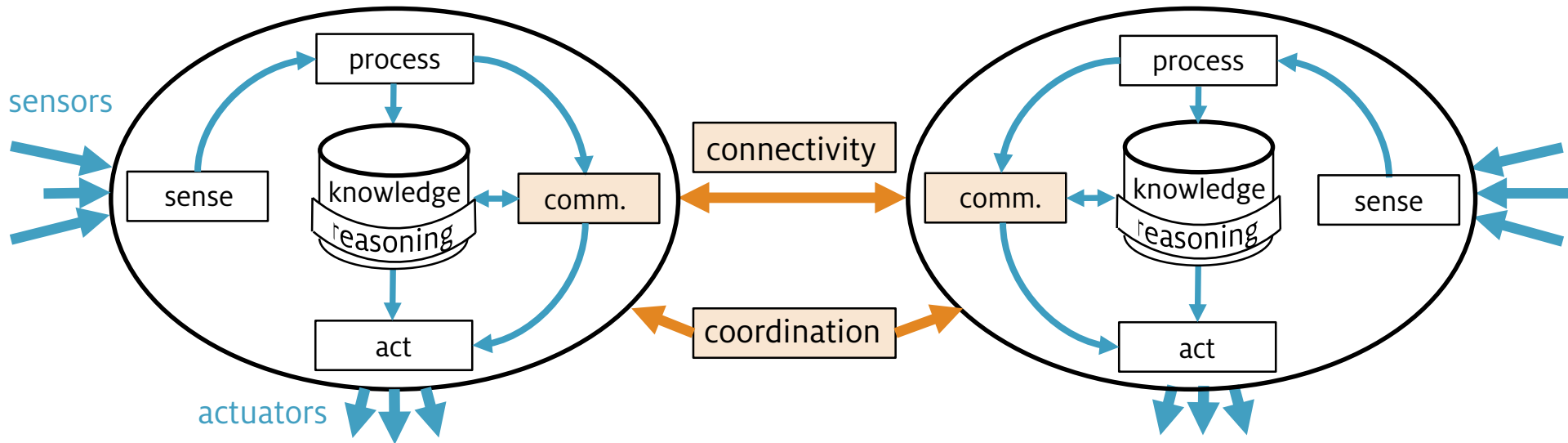
[Barciś, Bettstetter. Sandsbots: Robots that sync and swarm. *IEEE Access*, 2020.]

# From single Autonomous Agents



- Traditional architecture of autonomous agent
  - With **sense-process-act** cycle
  - Maintains **knowledge base with reasoning** capabilities

# To Multi-Robot Architecture



- Expanded data processing of individual robots by
  - Coordination of decision making
  - Robust wireless connectivity to transfer data with different QoS
  - Communication for optimized data distribution (what, when, to whom)

[Rinner, Bettstetter, Hellwagner, Weiss. [Multidrone systems: More than the sum of the parts](#). *IEEE Computer*, 2021.

# Terminology

- Robot is a **special kind of agent** (mostly) realized as a mechatronic construct
- Multi-robot system is a group of **robots operating in the same environment**
- **MRS coordination** can be classified wrt.
  - Cooperation: Do the robots cooperate to solve a problem?
  - Knowledge: How much knowledge do have robots about each other
  - Coordination: How much joint decision making is enforced?
  - Organization: What kind of decision structure is employed?
- Emphasis on MRS consisting of autonomous robots that **collaborate** in order to achieve a **common global goal**

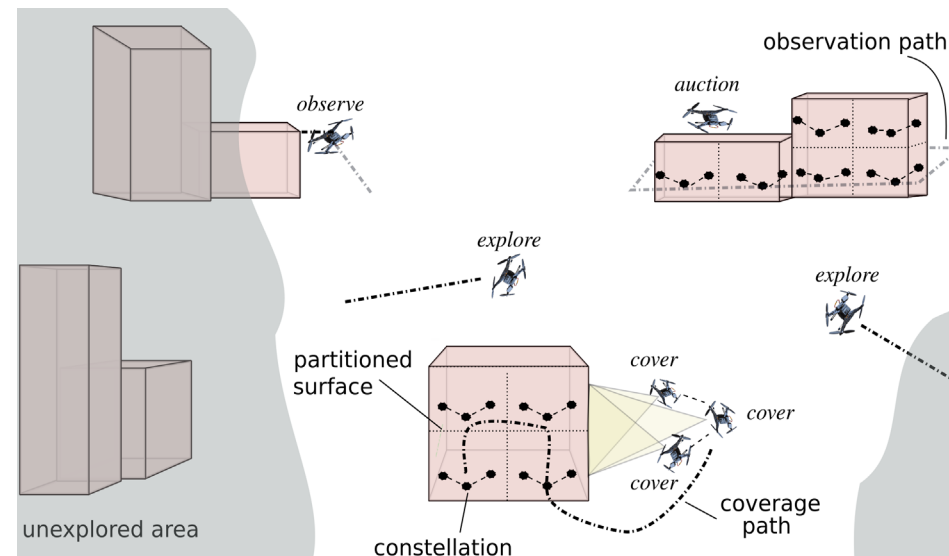
[K.Geihls. [Engineering Challenges Ahead for Robot Teamwork in Dynamic Environments](#). *Applied Sciences*, 2020.]

# Multi-robot Application Scenario

- Drones equipped with cameras **collect data about environment**

- Drones take on **different roles**

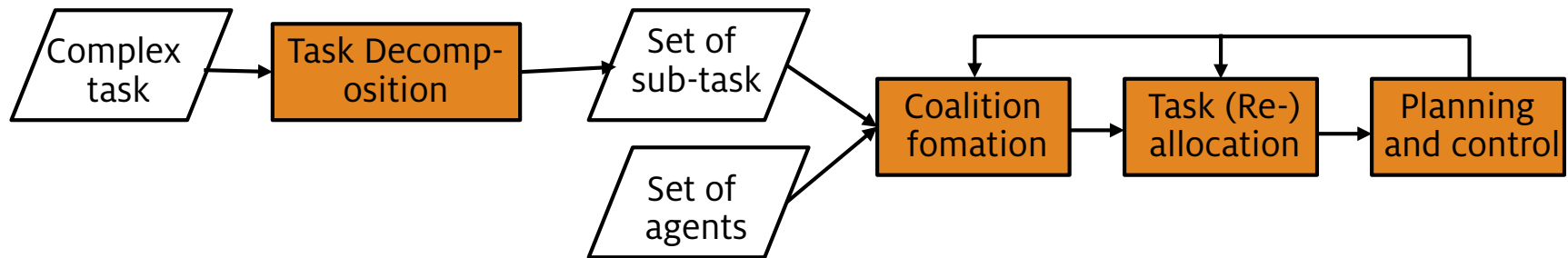
- Explore unknown areas
- Detect and partition objects
- Analyze partitions in joint constellations
- Move along observation paths



- Example for **generic MRS coordination tasks**

[Mazdin, Rinner. [Distributed and Communication-Aware Coalition Formation and Task Assignment in Multi-Robot Systems](#).

# MRS Work Flow



- Four main **design blocks** for MRS
  - Task decomposition: How to divide complex tasks into sub-tasks?
  - Coalition formation: How to form teams for sub-tasks?
  - Task allocation: How to assign sub-tasks to agents for execution?
  - Task execution: How to plan and control actions to complete sub-tasks?
- Varying **degree of automation** for design blocks
  - Human vs. robot
  - Offline vs. online

[Rizk, Awad, Tunstel. [Cooperative Heterogeneous Multi-Robot Systems: A Survey](#). *ACM Computing Surveys*, 2019.]

# Task Decomposition

- Task decomposition typically requires **domain knowledge** and considers **robot capabilities**
- Complexity, amount and interdependency of sub-tasks has impact on other blocks
  - Multi-agent tasks require collaboration of multiple robots
- Simple **decomposition strategies**
  - Spatial partitioning: decompose the environment
  - Temporal partitioning: decompose into sequence of sub-tasks
- Decomposition often performed offline and manually

# Coalition Formation

- Coalition formation typically casted as (multi-criterion) **optimization problem** with distinction into
  - Single or multi-robot tasks
  - Static or dynamic teams
  - Deterministic or uncertain robots' behavior; decentralized approaches
- Search algorithms often adapted to coalition formation problems, eg.,
  - Ant colony optimization, particle swarm optimization, evolutionary algorithms
- Combined coalition formation and task allocation
  - Market-based approaches, voting games
  - Reinforcement learning frameworks

# Task Allocation

- Task allocation is **well-investigated** with many approaches, but MRS introduce specific constraints (eg., spatial, temporal, sensing and actuation)
- Examples of **MRS-specific task allocation** approaches
  - Optimization or approximation travel distance of robots
  - Auctioning algorithms
  - Multi-agent reinforcement learning, distributed constraint optimization
- Combined coalition formation and task allocation typically improves performance at additional computation cost

# Planning and Control

- MRS planning and control (decision making) determines sequence of actions agents should perform to complete their assigned task
- Multiple frameworks for solving decision-making problems, including RL, game theory, swarm intelligence, and graph-theoretic models.

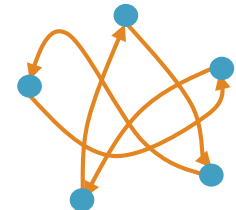
Model	Degree of Scalability	Degree of Heterogeneity	Degree of Communication
Swarm Intelligence	High	Low	Low
Multi-agent MDP	Medium	Medium	Medium
Decentralized MDP	Medium	Medium	Medium
Multi-agent POMDP	Medium	Medium	High
Decentralized POMDP	Medium	Medium	High
Interactive POMDP	Low	Medium	High
Partially Observable Stochastic Games	Low	High	Medium

[Rizk, Awad, Tunstel. [Cooperative Heterogeneous Multi-Robot Systems: A Survey](#). *ACM Computing Surveys*, 2019.]

# Team Behavior Examples

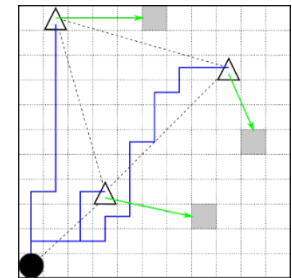
## 1. Collision-free and efficient path planning

- Fast and safe constellation changes for many drones
- Optimize for mission time and energy consumption



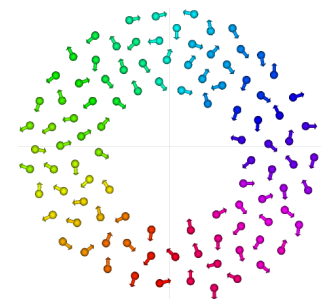
## 2. Cooperative route planning for surveillance

- Multi robot routes for persistent surveillance with latency, idleness and energy constraints
- Maintain continuous or intermittent connectivity



## 3. Swarming and synchronization

- Emergent, self-organizing team behavior
- Couple oscillators for joint synchronization and motion



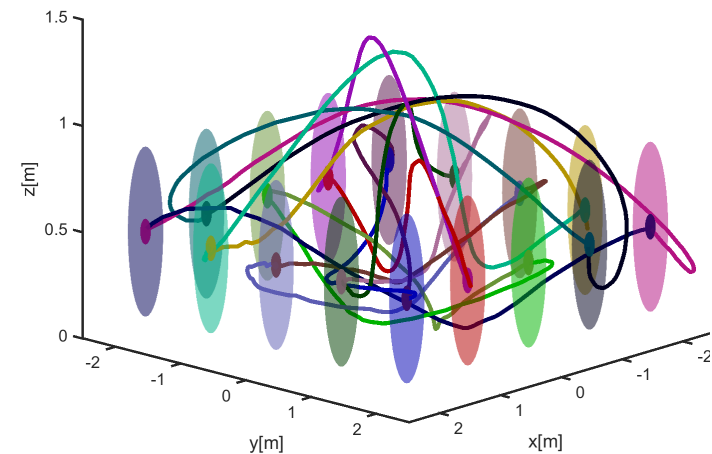
[Dronehub Klagenfurt <https://uav.aau.at>]

# Motion Planning in MRS

- Planning the **movement of robots** to reach a target
  - **Path planning**: determine path (trajectory) from A to B
  - **Route planning**: navigate in environment along multiple (way) point
- Variations in **modelling** environment and robots, e.g.,
  - Continuous models, grids, graphs
  - Robot dynamics, linear movements models, discrete movement
- Constraints and objectives
  - Collision free movement, space limitations
  - Connectivity (permanent or intermittent)
  - Energy consumption, movement time, ...
- Motion planning in MRS as **complex coordination problem**

# Multi-drone Constellation Change

- Many drones **simultaneously move from start to end constellation**
  - avoiding collisions among each other
  - reducing transition time and energy
- Two-step path planning approach  
“Snap-optimized MPC with potential field extension (SOMPF)”
  - Compute **initial, individual trajectories** with model predictive control (MPC) and **reduce potential collisions** with potential fields
  - Generate **final trajectories** by minimizing snap within **dynamic volume constraints**



# Initial Trajectories

- **System dynamics** of drone  $i$  with discretization step size  $h$

$$\begin{aligned}\mathbf{p}_i[k+1] &= \mathbf{p}_i[k] + h\mathbf{v}_i[k] + \frac{h^2}{2}\mathbf{a}_i[k] \\ \mathbf{v}_i[k+1] &= \mathbf{v}_i[k] + h\mathbf{a}_i[k]\end{aligned}$$

with physical limits on position  $\mathbf{p}_i$ , velocity  $\mathbf{v}_i$  and acceleration  $\mathbf{a}_i$

- **Collision constraints** at time points  $k$

$$\|\Theta^{-1}(\mathbf{p}_i[k] - \mathbf{p}_j[k])\|_2 \geq r_{min} + \varepsilon_{ij}, \quad \forall i, j, k | i \neq j$$

with scaling matrix  $\Theta$  and relaxation factor  $\varepsilon_{ij}$

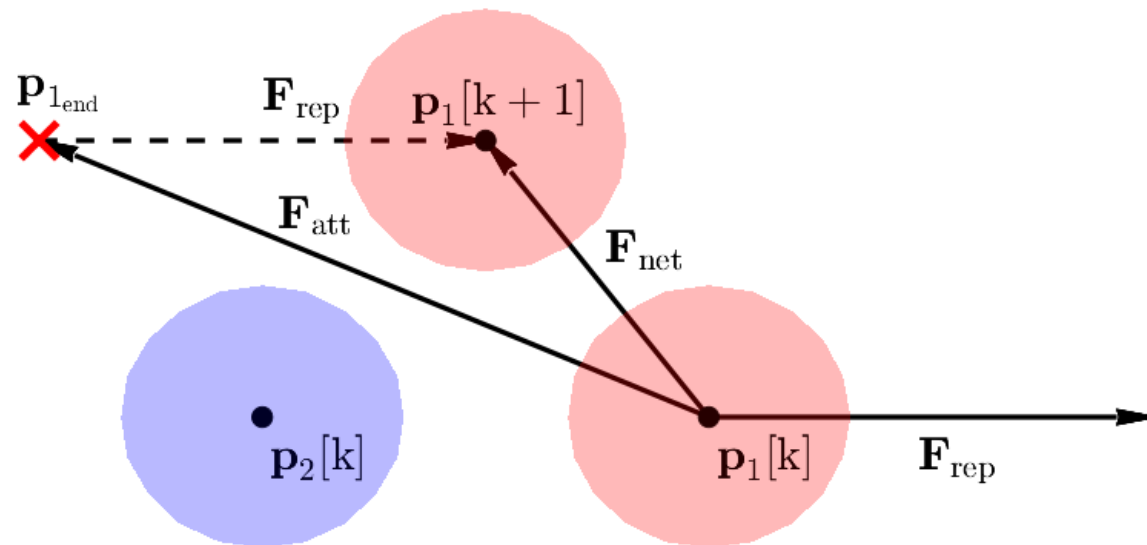
- Compute the predicted accelerations  $\mathbf{U}_i$  over MPC time horizon by **solving a quadratic program**

$$\begin{aligned}\min_{\mathbf{U}_i} & \mathbf{U}_i^T \mathbf{H} \mathbf{U}_i + \mathbf{f}^T \mathbf{U}_i, \forall i \\ \text{s.t.} & \mathbf{A} \mathbf{U}_i \leq \mathbf{b}\end{aligned}$$

Cost functions ( $\mathbf{H}$  and  $\mathbf{f}$ ) governs transition of each agent

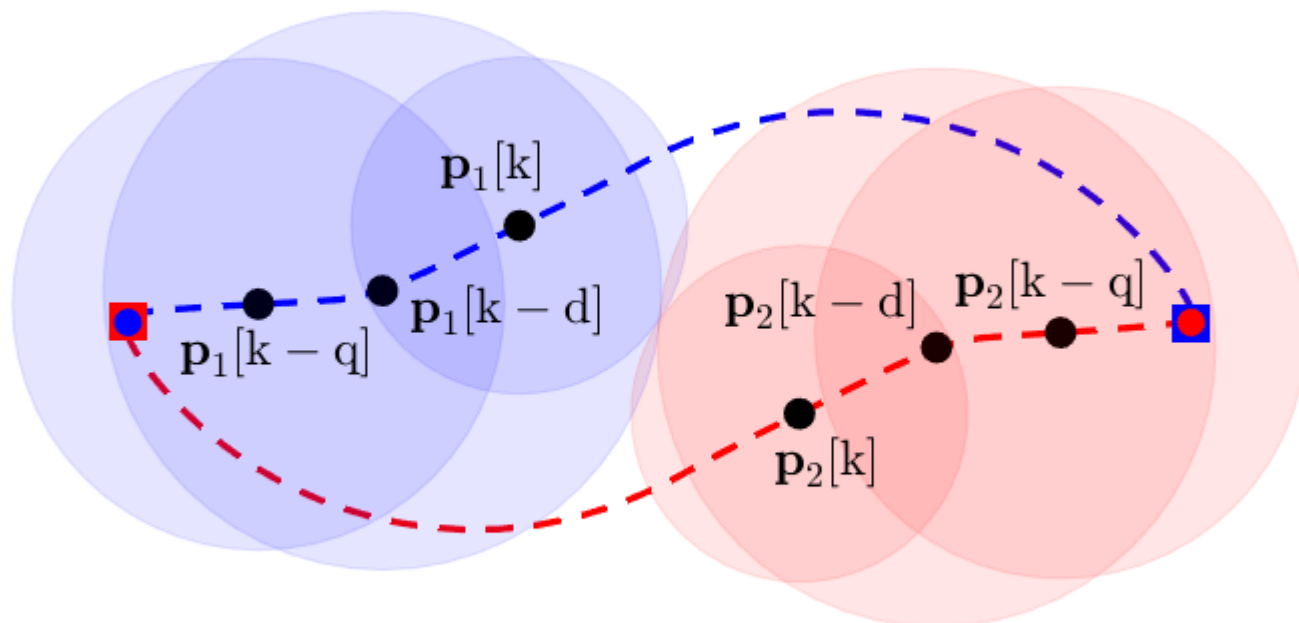
# Collision Avoidance

- If collision at newly propagated  $\mathbf{p}_i[k + 1]$  is detected  
apply **potential fields to bypass collision**



# Trajectory Refinement

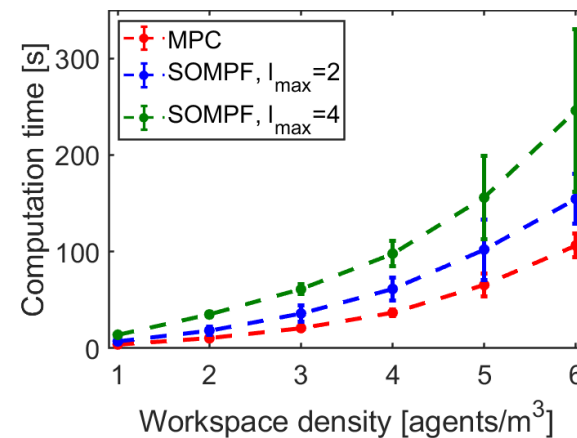
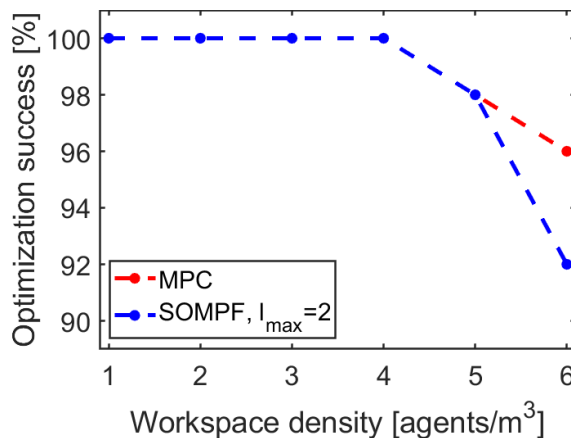
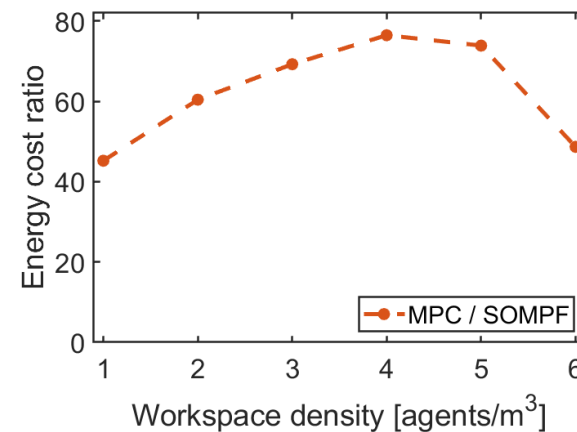
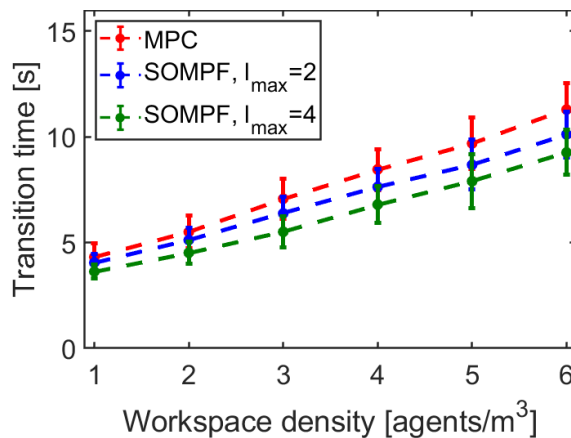
- Perform **snap minimization** with **dynamic volume constraints**



- Compute the maximum **intersection-free corridor** (spheres) at each time step
- Refined trajectories are **faster** and **more energy-efficient**

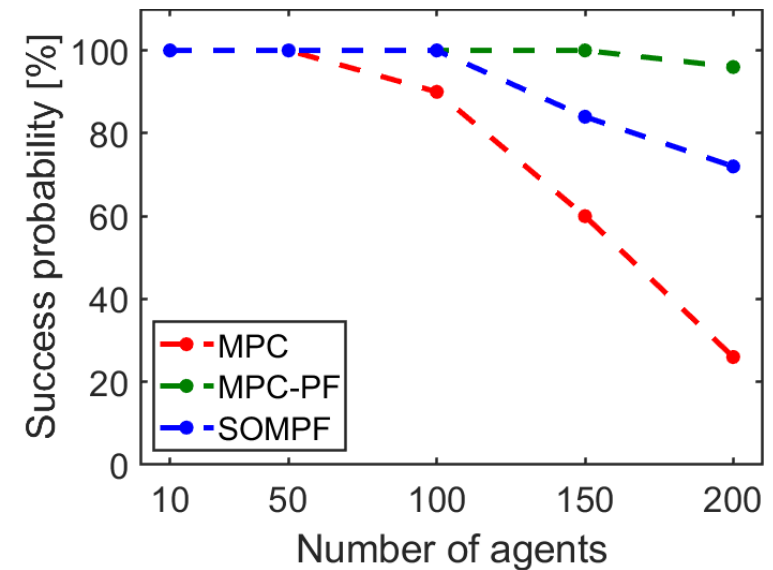
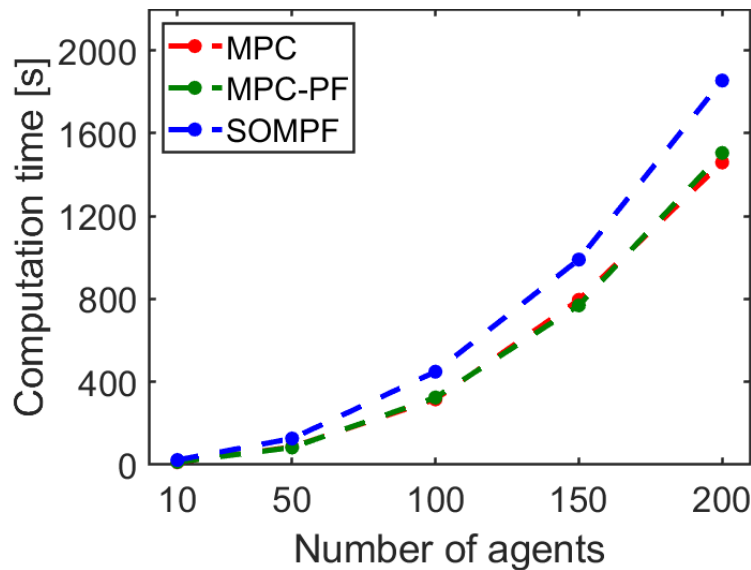
# Performance Evaluation

- Constellation changes within a fixed flight volume and **varying agent density**



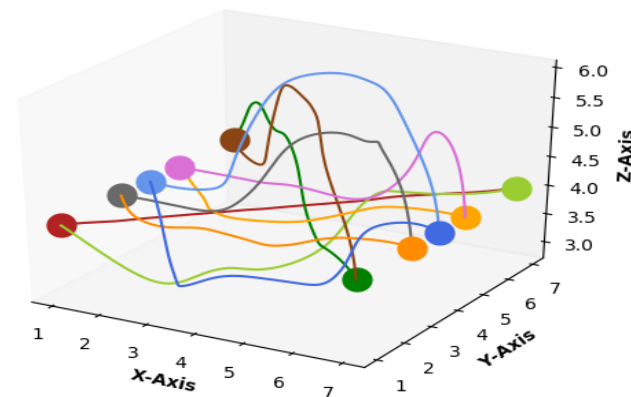
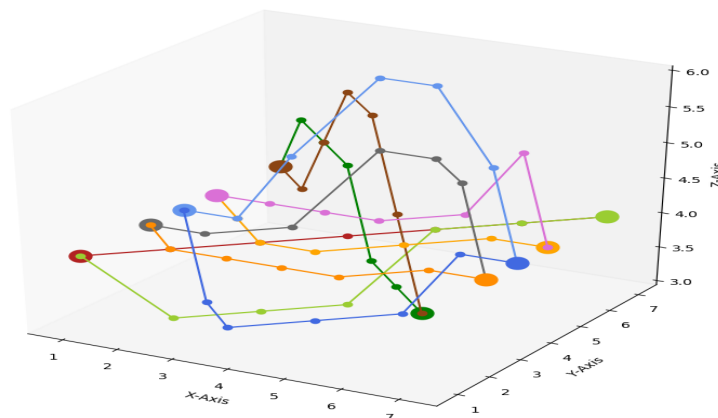
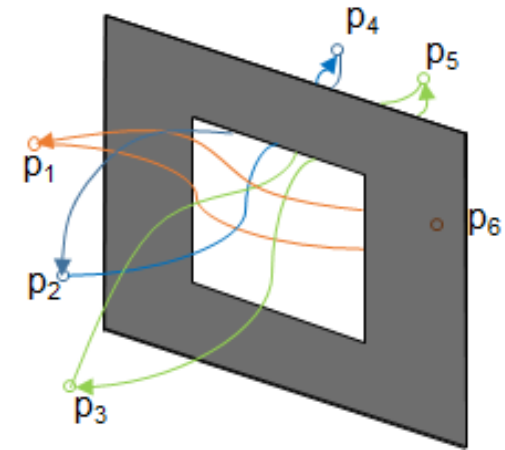
# Performance Evaluation (2)

- Constellation changes with **varying agents** and constant agent density (1 agent/m<sup>3</sup>)



# Constellation Change with Obstacles

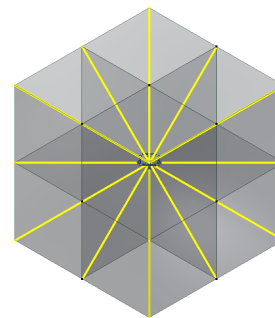
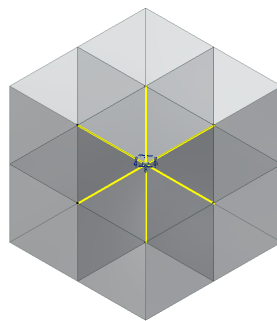
- $N$  drones simultaneously move in confined environments
- Path planning approach
  - Apply discrete multi-agent path planning (enhanced conflict-based search)
  - Generate trajectories within volume of discrete path (following snap minimization)



[Beyoglu, Weiss, Rinner. [Multi-Agent Path Planning and Trajectory Generation for Confined Environments](#). In *Proc. ICUAS*, 2022.]

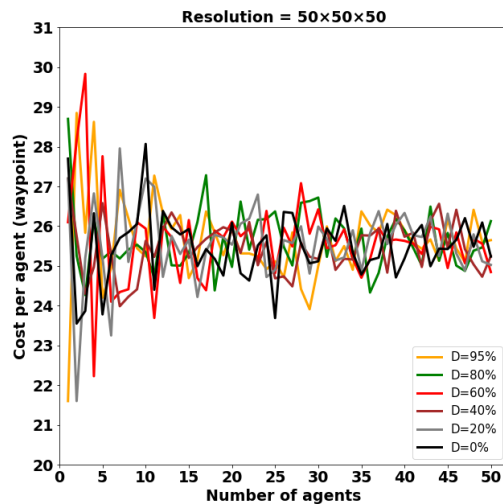
# Waiting Events to Avoid Collision

- Waiting events are **problematic with discrete planning**
  - If no conflict-free movement to any neighboring cell is possible, agents need to wait (“waiting event”)
  - Waiting events **impede smooth and energy-efficient trajectory** generation (deceleration, hovering and acceleration)
- Extend the available movement actions at each discrete planning step
  - Diagonal movement results in 26 potential movement actions within discretized 3D grid

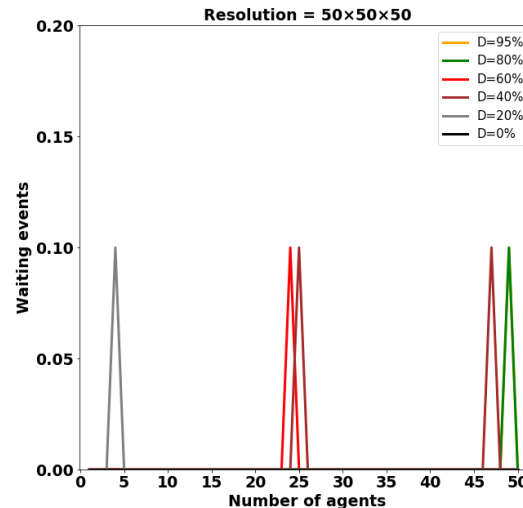


# Simulation Results

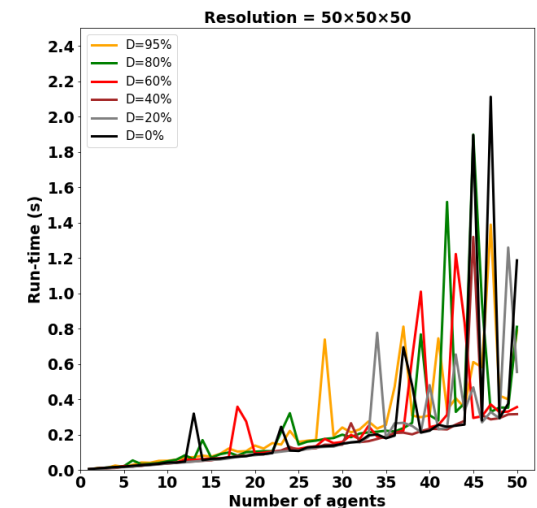
- Performance in environments with randomly placed obstacles and fixed spatial resolution
  - Mean values from 10 simulation runs



Average path length



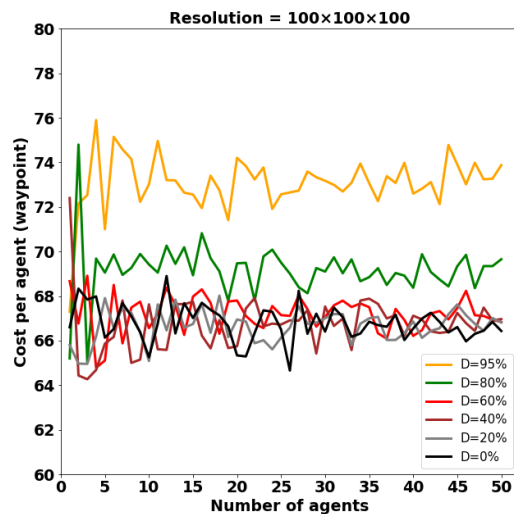
Introduced waiting events



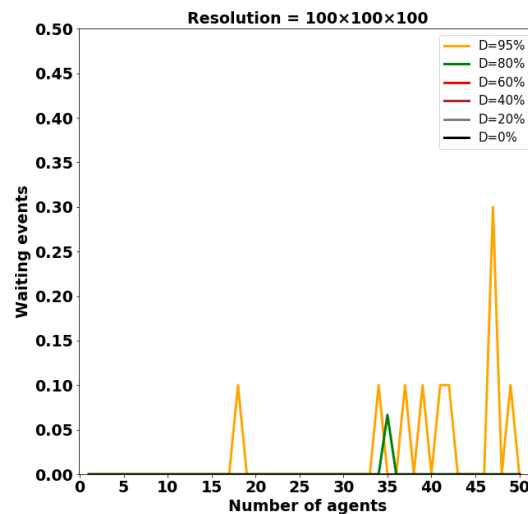
Planning time

# Simulation Results (2)

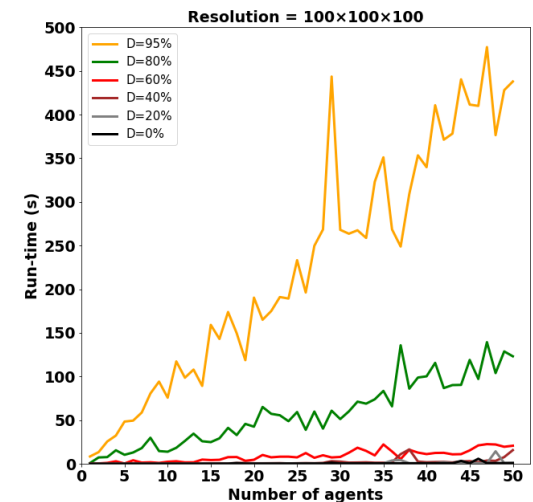
- Performance in environments with **varying window border size** and fixed spatial resolution
  - Mean values from 10 simulation runs



Average path length



Introduced waiting events

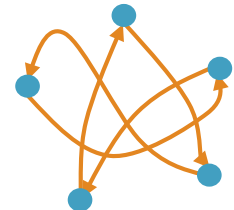


Planning time

# Team Behavior Examples

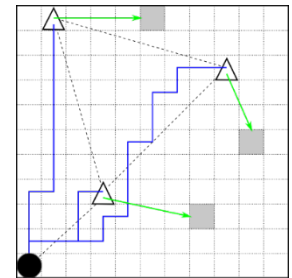
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- Fast and safe constellation changes for many drones
- Optimize for mission time and energy consumption



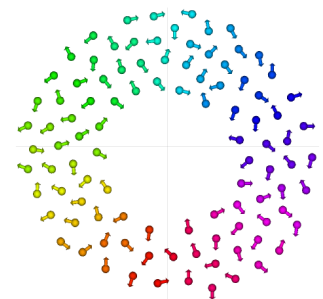
## 2. Cooperative route planning for surveillance

- Multi robot routes for persistent surveillance with latency, idleness and energy constraints
- Maintain continuous or intermittent connectivity



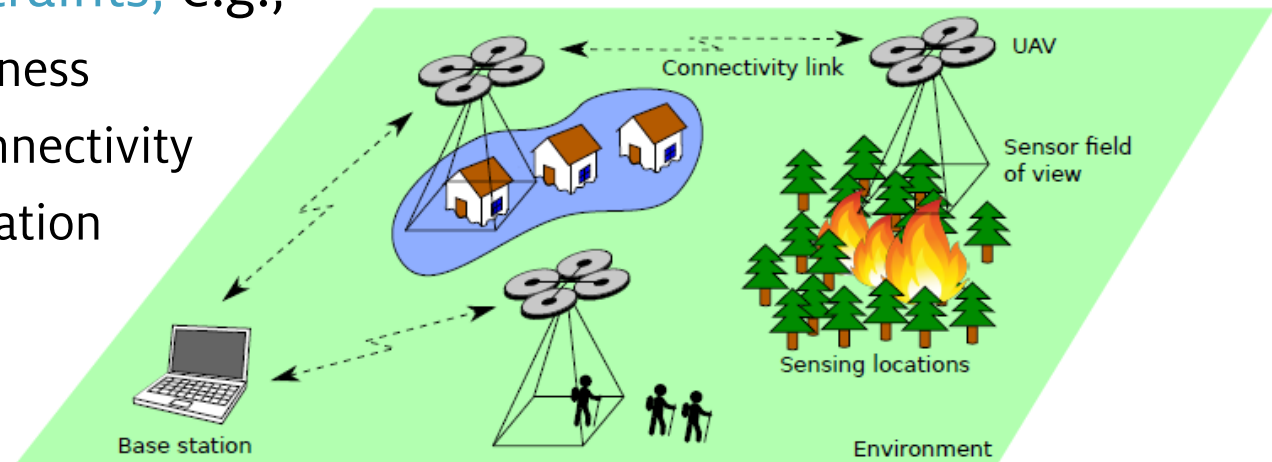
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# Motion Planning for Surveillance

- Continuously monitor environment while maintaining **multiple constraints**, e.g.,
  - Sensing idleness
  - Network connectivity
  - Energy limitation

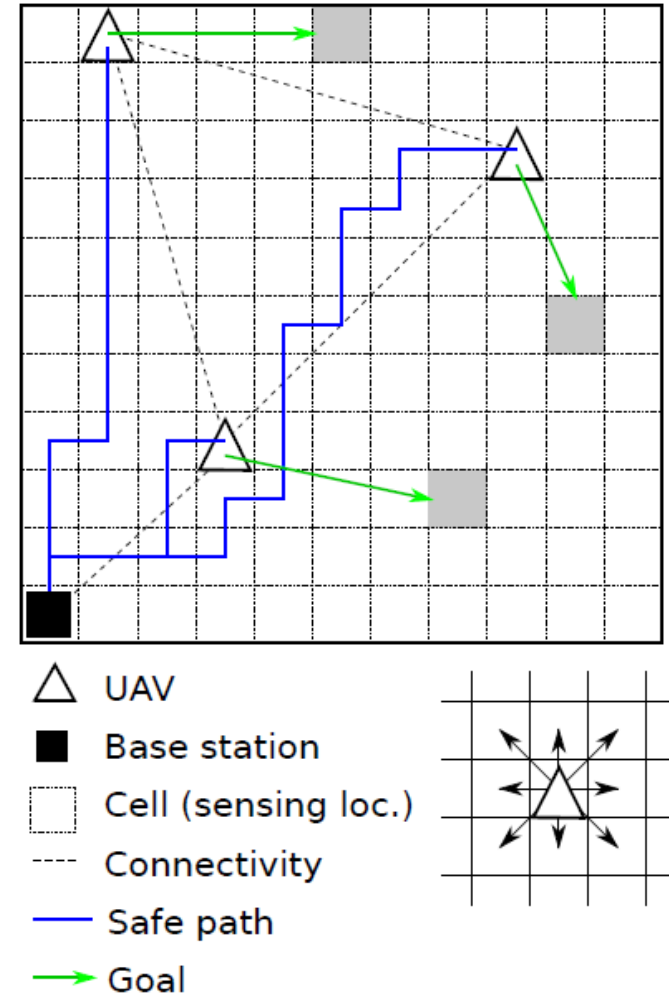


- Persistent surveillance (PS) or patrolling problem
  - Requires **coordination of robots' movement** in space and time
  - Fundamental problem for various MRS applications

[Scherer, Rinner. [Multi-robot persistent surveillance with connectivity constraints](#). *IEEE Access*. 2020]

# PS with Persistent Connectivity

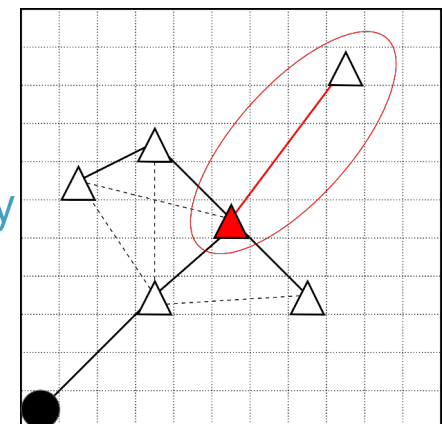
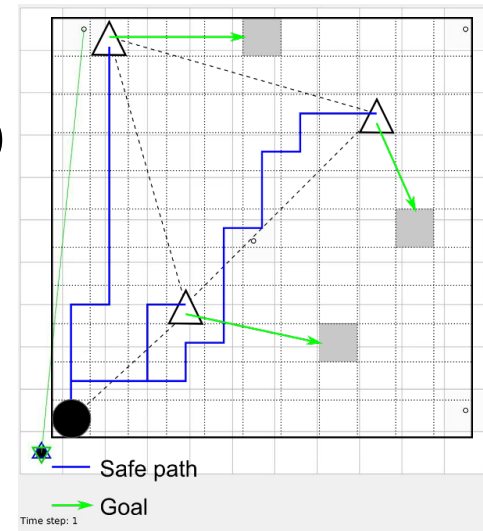
- Plan paths that **minimize worst idleness** and keep **network connected**
  - Grid-based environments (partitioned into convex areas) and synchronous movement
  - Intermediate (relay) robots for **maintaining connectivity** (distance between robots)
  - If **energy is limited** return periodically to BS for recharging (along safe path)
  - Path planning is NP hard (proof by transformation to 3SAT)
- Investigate new **motion planning heuristics** with different planning horizon and coordination
  - Short vs. full horizon planning
  - Individual vs. cooperative planning



# Short Horizon Planning (SH)

- Adopted **goal-based heuristic** [Nigam 2012]
  - Each drone  $u$  moves to cell  $c$  with highest  $A(u, c)$ 

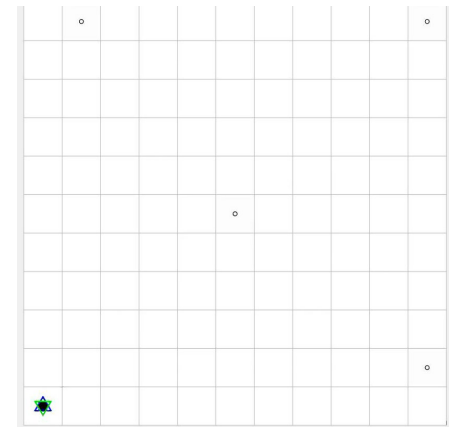
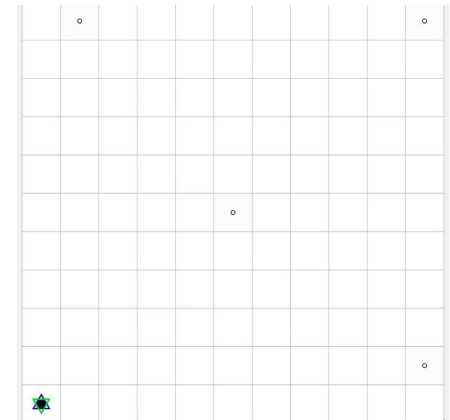
$$A(u, c) = \underbrace{I(c)}_{\text{Idleness}} + w_0 \cdot \underbrace{\text{dist}(u, c)}_{\text{Distance to cell}} + w_1 \cdot \underbrace{\min_{v \neq u} \text{dist}(v, c)}_{\text{Minimum distance to other drones } v}$$
  - Weights  $w_0$  and  $w_1$  initially determined  
 $A(u, c)$  values updated at each iteration
- Extended by **safe paths for each drone** to guarantee return to base station
  - with **remaining energy** without losing **connectivity**
  - If one drone reaches its energy limit, all drones move along safe paths back to base



[Nigam et al. [Control of multiple UAVs for persistent surveillance: Algorithm and flight test results](#). *IEEE Trans. on Control Systems Technology*. 2012]

# Cooperative Planning

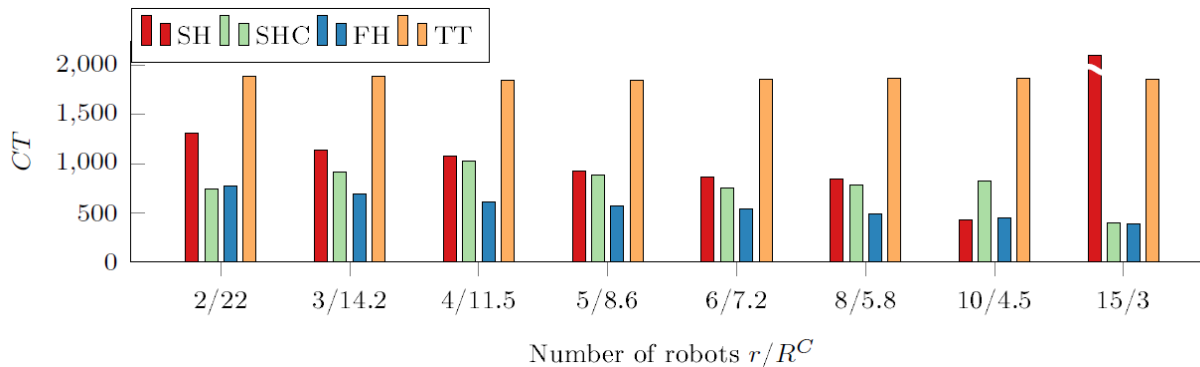
- Avoid **limitations** of non-cooperative SH planning, e.g.,
  - Deadlocks (oscillations and mutual blocking)
- **Short horizon cooperative (SHC)** planning
  - Select robots for next sensing locations
  - Coordinate movement by graph matching (from current to next sensing configuration)
- **Full horizon (FH)** planning
  - Leader robot traverses tour through all sensing locations, other robots relay data to BS
  - If many robots available, several leader robots (partitioning)
  - Planning cycle for complete environment



[Scherer, Rinner. [Short and Full Horizon Motion Planning for Persistent multi-UAV Surveillance with Energy and Communication Constraints](#). In *Proc IROS*. 2017]

# Comparison of Planning Algorithms

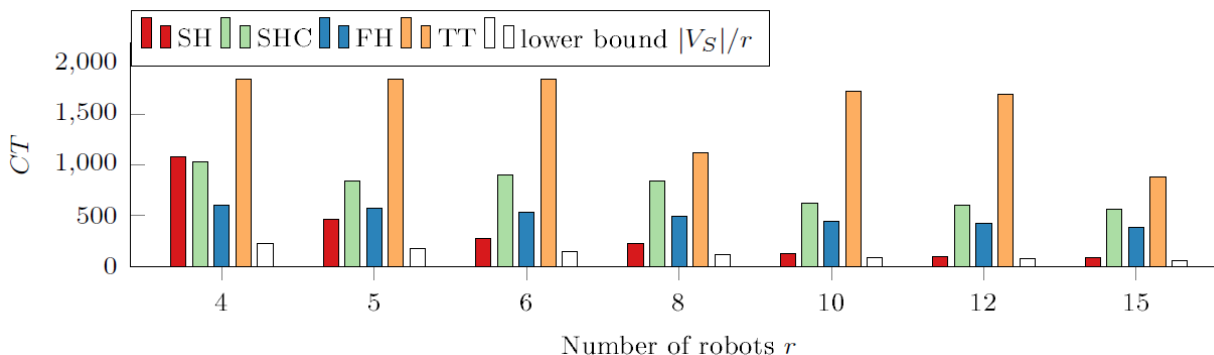
- Simulation study on  $30 \times 30$  cells
    - First coverage time (CT) of entire area
- Varying number of robots with decreasing and fixed comm. range  $R^C$



## Strong comm. constraints

(all robots required for remote cells)

- FH outperforms others
- SH fails to cover area for 15 robots
- TT tree traversal for partitioned areas as reference



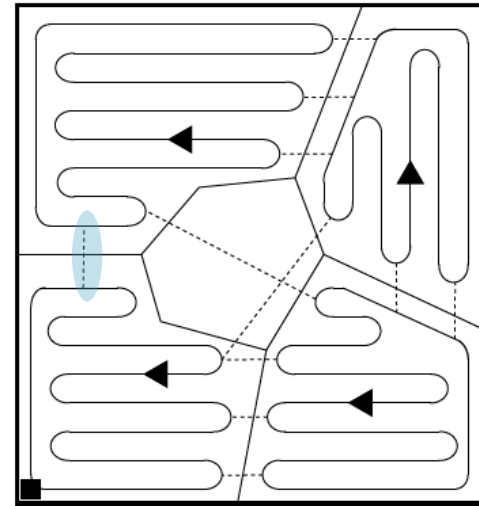
## Weak comm. constraints

(4 robots required for remote cells)

- SH approaches lower bound
- TT tree traversal for partitioned areas as reference

[Scherer, Rinner. [Multi-robot persistent surveillance with connectivity constraints](#). *IEEE Access*. 2020]

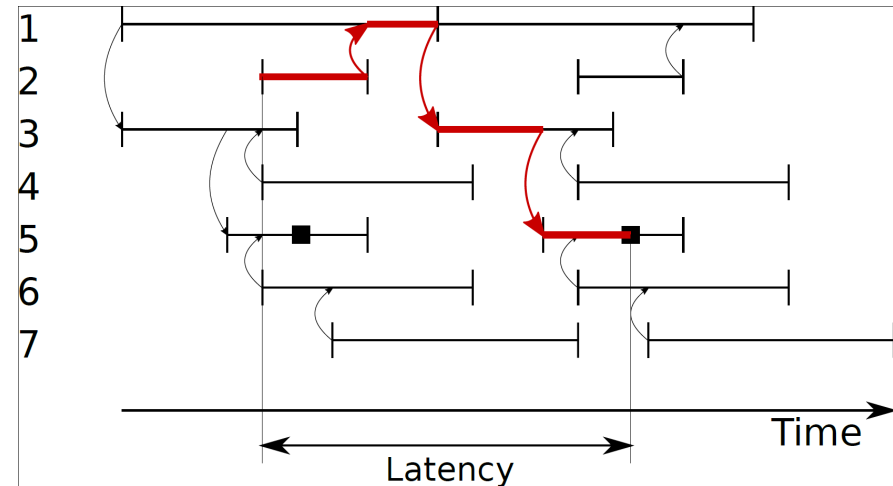
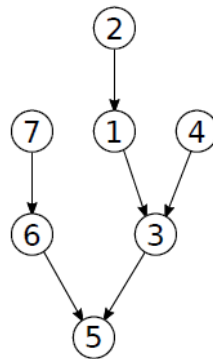
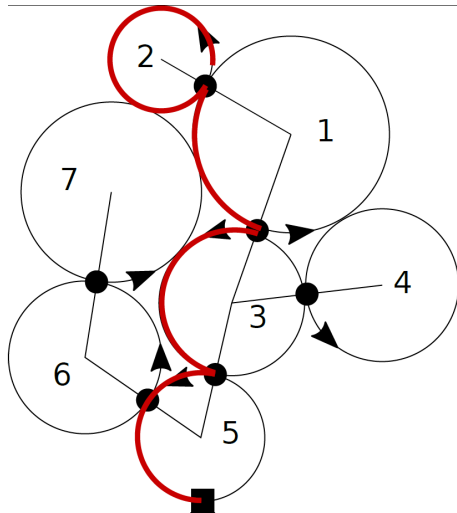
- Schedule movement along given tours to **minimize worst idleness** and data delivery **latency**
  - Data transfer only at **meeting points** (store-and-forward)
  - Who should meet when and where
  - Minimum delay scheduling is NP hard (proof by transformation to 3SAT)
- Investigate new **robot scheduling algorithms** for given tours
  - Selecting travel direction and meeting points
  - Executing schedules onboard robots



[Scherer, Rinner. [Multi-Robot Patrolling with Sensing Idleness and Data Delay Objectives](#).  
*J. Intelligent & Robotic Systems*. 2020]

# Scheduling based on Tour Graphs

- Model data transfers among patrolling robots as tour



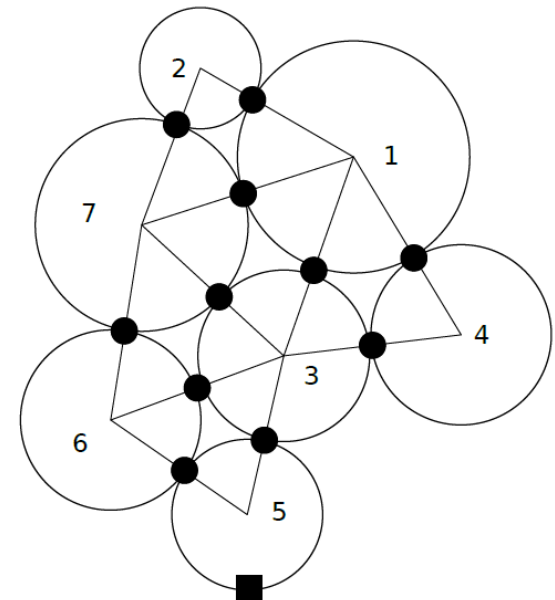
- Robots patrol environment along given tours
- Data transfer via meeting points represented as graph (here tree)
- Determine for each robot when to move, wait and transfer
- Move along longest tour without waiting
- Construct schedule beginning with base station

[Scherer, Rinner. [Multi-Robot Patrolling with Sensing Idleness and Data Delay Objectives](#).  
*J. Intelligent & Robotic Systems*. 2020]

# Various Problem Instances

## Minimize latency for given tours and bounded idleness

1. Select tour directions
  - Input: tour tree
  - Output: directions, schedule
2. Select tree (NP hard)
  - Input: tour graph, directions
  - Output: tree, schedule
3. Select tree and tour directions (NP hard)
  - Input: tour graph
  - Output: tree, directions, schedule
4. Select tree, meeting points and tour direction (NP hard)
  - Input: tour multi-graph (multiple meeting points between tours)
  - Output: tree, directions, schedule



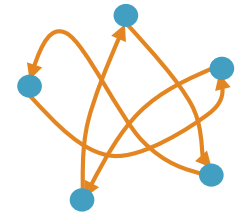
## Minimize idleness for given tours and latency constraint

[Scherer, Rinner. [Multi-UAV Surveillance with Minimum Information Idleness and Latency Constraints](#). *IEEE Robotics and Automation Letters*. 2020]

# Team Behavior Examples

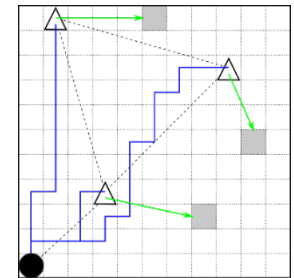
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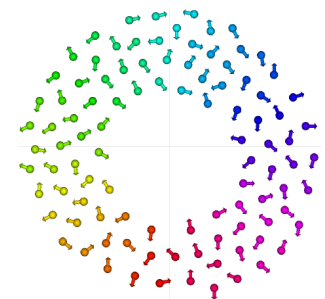
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- Multi robot routes for persistent surveillance with latency, idleness and energy constraints
- Maintain continuous or intermittent connectivity



## 3. Swarming and synchronization

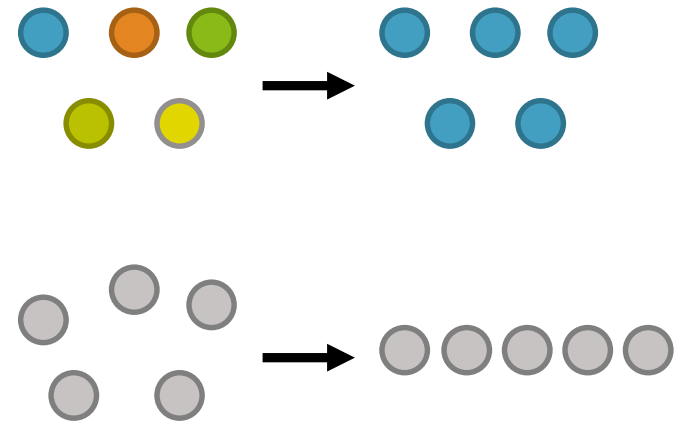
- Emergent, self-organizing team behavior
- Couple oscillators for joint synchronization and motion



# Selforganization for Drone Swarms

[lead by c. Bettstetter]

- Synchronization
  - Coordination of robots to achieve order in **time domain**
  - Adjustment of **phases**  $\phi_i$
- Swarming
  - Coordination of robots to achieve order in **space domain**
  - Adjustment of **locations**  $x_i$
- **Swarmalators**
  - Unified model where robot's phase and location are mutually coupled
  - Emergent space-time patterns



[O'Keeffe, Hong, Strogatz. [Oscillators that sync and swarm](#). *Nature Communications*. 2017]

[Barcis, Bettstetter. [Sandsbots: Robots That Sync and Swarm](#). *IEEE Access*. 2020]

# Swarmalators

## Synchronization

The phases  $\phi_i$  of robots influence each other.

E.g.: Phases synchronize to a common value, or “desynchronize” to differing values (splay states).

## Swarming

The locations  $x_i$  of robots influence each other.

E.g.: Robots physically attract or repel each other based on their distance.



**Swarmalators:** bidirectional coupling between sync and swarming

The phases  $\phi_i$  influence the movements  $\dot{x}_i$ , and  
the positions  $x_i$  influence the phase dynamics  $\dot{\phi}_i$ .

E.g.: Entities with similar phases may attract or repel each other stronger, and close-by entities may synchronize faster.

# Swarmalator Model

- Phase-dependent movement

- $N$  nodes indexed by  $i$
- Location  $x_i$  and distance  $x_{ij}$
- Phase  $\phi_i$  and phase diff  $\phi_{ij}$

$$\dot{\mathbf{x}}_i = \frac{1}{N} \sum_{j \neq i}^N [\underbrace{\mathbf{I}_1(\mathbf{x}_{ij})}_{\text{Attraction}} F(\phi_{ij}) - \underbrace{\mathbf{I}_2(\mathbf{x}_{ij})}_{\text{Repulsion}}] \quad \text{with} \quad F(\phi_{ij}) = 1 + J \cos \phi_{ij}$$

- Location-dependent synchronization

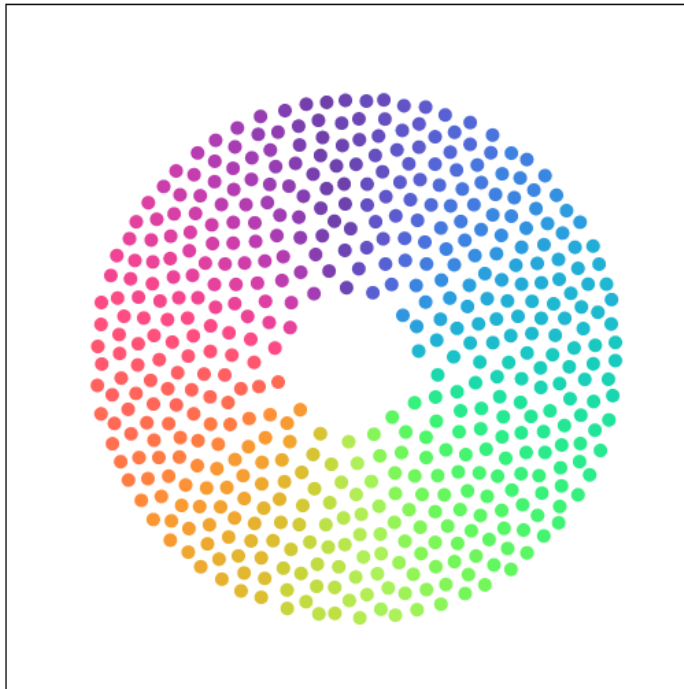
*Behavior is governed by two parameters  $J$  and  $K$ .*

$$\dot{\phi}_i = \frac{K}{N} \sum_{j \neq i}^N \underbrace{H(\phi_{ij})}_{\text{Attraction}} G_\phi(\mathbf{x}_{ij}) \quad \text{with} \quad G_\phi(\mathbf{x}_{ij}) = \frac{1}{\|\mathbf{x}_{ij}\|}$$

[O'Keefe, Hong, Strogatz. [Oscillators that sync and swarm](#). *Nature Communications*. 2017]

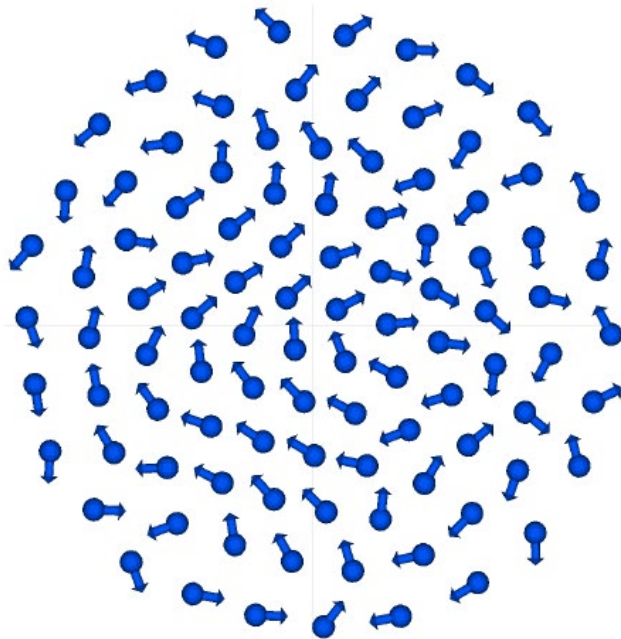
# Complexity explorable “Swårmalätørs”

[by D. Brockmann]



[Brockmann: Complexity explorable: Swårmalätørs - Pattern that emerge when collective motion and synchronization entangle, [complexity-explorables.org](https://complexity-explorables.org), 2021.]

# Swarmalator Patterns



Static sync

$$(J, K) = (0.1, +1)$$

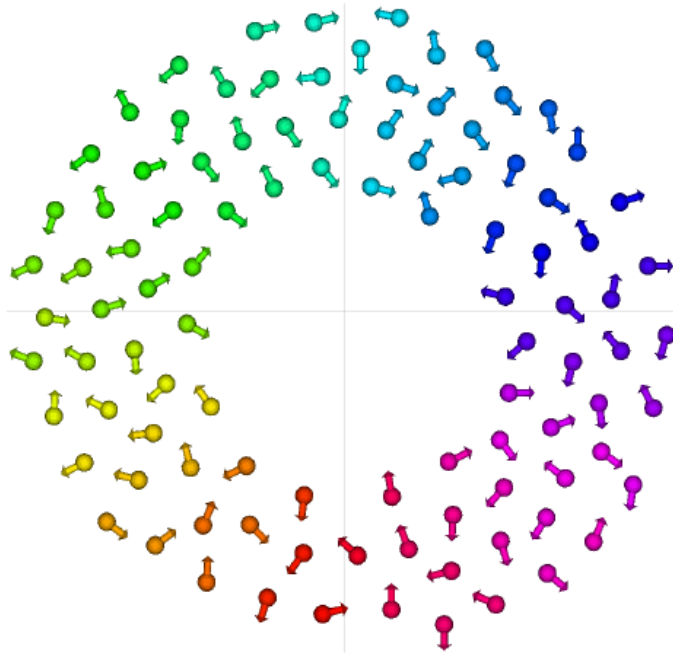


Static async

$$(J, K) = (0.1, -1)$$

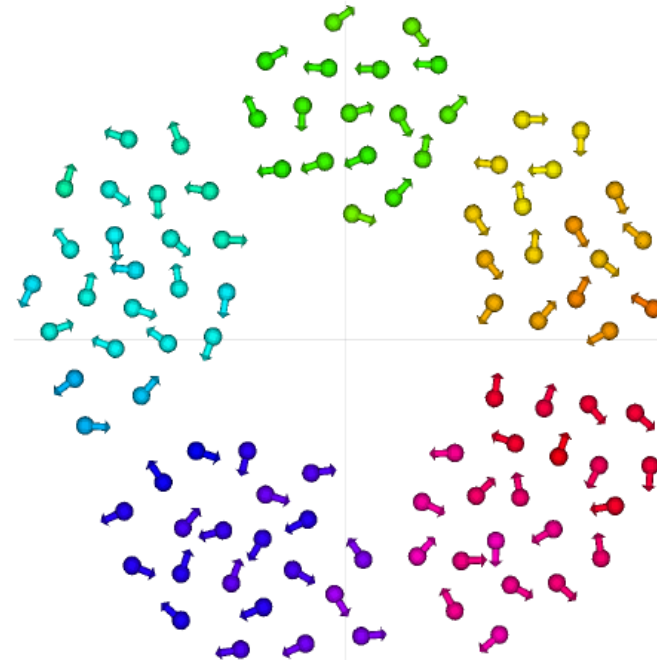
[O'Keefe, Hong, Strogatz. [Oscillators that sync and swarm](#). *Nature Communications*. 2017]

# Swarmalator Patterns (2)



Static phase wave

$$(J, K) = (1, 0)$$



Splintered phase wave

$$(J, K) = (1, -0.1)$$

[O'Keefe, Hong, Strogatz. [Oscillators that sync and swarm](#). *Nature Communications*. 2017]

# Swarmalators for Drone Swarms

[lead by c. Bettstetter]

- From theory to practice
  - How to **adapt** the swarmalator model for use in robotics?
  - Does the adapted model lead to **identical** patterns?
- **Limitations** of real multi-robot systems
  - Movement constraints and speed limitations
  - Collision avoidance
  - Interactions at discrete times via messages
  - Message loss and delay
  - Limited communication range

[Schilcher, Schmidt, Vogell, Bettstetter: [Swarmalators with stochastic coupling and memory](#).  
Proc. IEEE Intern. Conf. on Autonomic Computing and Self-Organizing Systems (ACSOS), 2021.]

[Barciś, Barciś, Bettstetter: [Robots that sync and swarm: A proof of concept in ROS 2](#).

B.Rinner Proc. IEEE Intern. Symp. on Multi-Robot and Multi-Agent Systems (MRS), 2019.]

# Deployment on Drones



Ground robot deployment: [Barcis et al. [Robots that Sync and Swarm: A Proof of Concept in ROS 2](#). In *Proc MRS*. 2019]

# Lessons Learnt

- Complexity
  - Multi-robot systems perform highly interdependent tasks
  - Interdisciplinary research for tackling complexity
- Methodology
  - Experimental research with multi-robot systems is challenging
  - Interesting feedback from engineering work to basic research
- Non-technical issues
  - Safety, legal, ethical and regulatory aspects need to be considered
- Perseverance

# Conclusion

- Two step **path planning** for free and confined environments
- Heuristic **route planning** for surveillance with connectivity constraints
- Swarmalators for **emerging synchronization and swarming**
- Coordination **problems are challenging and fundamental for several MRS applications**
  - Aim for efficient heuristics with performance bounds
  - Rely on various (simplifying) assumptions
  - Provide still many open research questions

# Drone Research at Klagenfurt

- Started in 2008
- Developed into a **key research area**
  - 8 Profs
  - >20 PhDs & PostDocs
  - **Dedicated doctoral school**
- Covering various **research topics**
  - Autonomous navigation & coordination
  - Mission & path planning
  - Wireless communication
  - Interaction & various applications
- Opening Europe's largest **drone hall**
  - > 1000 m<sup>3</sup> flight space
  - Motion capturing & 5G connectivity



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- Pervasive Computing group  
<https://www.bernhardrinner.com>



- Dronehub Klagenfurt  
Profs. Bettstetter, Hellwagner, Weiss  
<https://uav.aau.at>

